2.7 Practice Set

- 1. What is a complex number?
- 2. Why does the product rule for radicals $(\sqrt{a} \cdot \sqrt{b} = \sqrt{ab})$ fail when both a and b are negative? Give an example.
- 3. Describe the technique for dividing complex numbers. How is it similar to rationalizing the denominator for radical expressions?
- 4. Describe the pattern for the powers of *i*.

Simplify each of the following expressions. Write answers as complex numbers a + bi.

5.
$$\sqrt{-48}$$

6.
$$\sqrt{-90}$$

7.
$$\sqrt{-3} \cdot \sqrt{-12}$$

8.
$$(5-8i)+(9+2i)$$

9.
$$(6+17i)-(3-4i)$$

10.
$$(-3i)(-11i)$$

11.
$$4i(5i-2)$$

12.
$$(4+5i)(3-7i)$$

13.
$$(5+7i)^2$$

14.
$$\frac{2}{i}$$

15.
$$\frac{1}{9+6i}$$

16.
$$\frac{4-i}{7+5i}$$

17.
$$(4.2 - 12.7i) - (1.35 + 2i)$$

18.
$$\left(\frac{3}{5} - \frac{4}{5}i\right) + \left(\frac{6}{7} + i\right)$$

19.
$$\left(\frac{1}{4} - \frac{3}{8}i\right)\left(\frac{1}{2} + \frac{3}{2}i\right)$$

20.
$$(1.8 + 1.7i)(3.1 + 4.3i)$$

21.
$$\frac{5.4+3i}{2-4.9i}$$

22.
$$i^{18}$$

23.
$$(-6i)^7$$

24.
$$i^{13} - i^8$$

25.
$$\frac{20+\sqrt{-125}}{15}$$

Distributed Practice Problems

Solve each of the following equations for the indicated variable.

26.
$$\sqrt{69-t}-t=3$$

$$27. \sqrt{y} - \sqrt{3y - 2} = -2$$

Perform the indicated operation and/or simplify each of the following. Assume that all variables represent positive real numbers and rationalize all denominators.

28.
$$\sqrt[4]{\frac{16}{27}}$$

$$29. \qquad \frac{\sqrt{3} - \sqrt{5}}{\sqrt{3} + \sqrt{5}}$$

29.
$$\frac{\sqrt{3} - \sqrt{5}}{\sqrt{3} + \sqrt{5}}$$
30.
$$\frac{\left(4a^{-3}b^{2}\right)^{\frac{1}{2}}}{\left(27x^{3}y^{-2}\right)^{-\frac{2}{3}}}$$