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THE NATURE OF SCIENCE AND PHYSICS

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Example

- Problem (E1.2):
A grocery store sells 5 lb bags of apples. You purchase four bags over the course of a month and weight the apples each time. (You obtain the following measurements: Week 1 weight, 4.8 lb ; Week 2 weight 5.3 lb ; Week 3 weight, 4.9 lb ; Week 4 weight, 5.4 lb.) You determine that the weight of the 5 lb has an uncertainty of ± 0.4 lb. What is the percent uncertainty of the bag's weight?

- Solution:

We have

$$A = 5 \text{ lb}$$

$$\delta A = 0.4 \text{ lb}$$

$$u_p = ?$$

The **percent uncertainty** of the weight

$$\begin{aligned} u_p &= (\delta A / A) \times 100 \% \\ &= (0.4 \text{ lbs} / 5 \text{ lbs}) \times 100 \% = 8 \% \\ &= \mathbf{8 \%} \end{aligned}$$

The weight of the apple is: **5 lb \pm 0.4 lb** or **5 lb \pm 8%**

Problem 1

- Problem (P1.2):

A car is traveling at a speed of 33 m/s. What is its speed in kilometers per hour?

- Solution:

$$v = 33 \text{ m/s}$$

$$v \text{ (km/h)} = ?$$

The **speed** of the car in kilometers per hour is

$$\begin{aligned} v &= 33 \text{ m/s} \left(1 \text{ km} / 1000 \text{ m} \right) \left(3600 \text{ s} / 1 \text{ h} \right) \\ &= 118.8 \text{ km/h} \\ &= \mathbf{120 \text{ km/h}} \end{aligned}$$

Problem 2

- Problem (P1.8):

The speed of sound is measured to be 342 m/s on a certain day. What is this in km/h?

- Solution:

$$v = 342 \text{ m/s}$$

$$1 \text{ km} = 1000 \text{ m}$$

$$1 \text{ h} = 3600 \text{ s}$$

$$v \text{ (km/h)} = ?$$

The **speed** of sound in kilometers per hour is

$$\begin{aligned} v &= 342 \text{ m/s} \left(1 \text{ km} / 1000 \text{ m} \right) \left(3600 \text{ s} / 1 \text{ h} \right) \\ &= 1231.2 \text{ km/h} \\ &= \mathbf{1230 \text{ km/h}} \end{aligned}$$

Problem 3

- Problem (P1.12):**

A good-quality measuring tape can be off by 0.50 cm over a distance of 20 m. What is its percent uncertainty?

- Solution:**

$$\delta L = 0.50 \text{ cm} \quad L = 20 \text{ m}$$

$$u_p = ?$$

Converting the **uncertainty** in distance into meters

$$\begin{aligned} \delta L &= 0.50 \text{ cm} \left(1 \text{ m} / 100 \text{ cm} \right) \\ &= 0.0050 \text{ m} \\ &= 0.0050 \text{ m} \end{aligned}$$

The **percent uncertainty** is given by

$$\begin{aligned} u_p &= (\delta L / L) \times 100 \% \\ &= (0.0050 \text{ m} / 20 \text{ m}) \times 100 \% \\ &= 0.025 \% \\ &= \mathbf{0.03 \%} \end{aligned}$$

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Problem 4

- Problem (P1.20):**

A person's blood pressure is measured to be 120 ± 2 mm Hg. Assuming the same percent uncertainty, what is the uncertainty in a blood pressure measurement of 80 mm Hg ?

- Solution:**

$$\delta S = 2 \text{ mm} \quad S = 120 \text{ mm} \quad D = 80 \text{ mm} \quad u_p = ? \quad \delta D = ?$$

The **percent uncertainty** for systolic blood pressure

$$\begin{aligned} u_p &= (\delta S / S) \times 100 \% \\ &= (2 \text{ mm} / 120 \text{ mm}) \times 100 \% = 1.667 \% \\ &= \mathbf{2 \%} \end{aligned}$$

Using this percent uncertainty, the **uncertainty** in diastolic blood pressure is

$$\begin{aligned} \delta D &= (u_p / 100 \%) D \\ &= (1.667 \% / 100 \%) 80 \text{ mm} = 1.3336 \text{ mm of Hg} \\ &= \mathbf{1 \text{ mm of Hg}} \end{aligned}$$

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Problem 5

- Problem (P1.22):
What is the area of a circle 3.102 cm in diameter?

- Solution:

$$r = 0.5 \times 0.03102 \text{ m}$$

$$A = ?$$

The **area** of the circle is

$$\begin{aligned} A &= \pi r^2 \\ &= (3.14159) [0.5 \times 0.03102 \text{ m}]^2 = 7.55741 \times 10^{-4} \text{ m}^2 \\ &= \mathbf{7.557 \times 10^{-4} \text{ m}^2} \end{aligned}$$

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Problem 6

- Problem (P1.28):
A car engine moves a piston with a circular cross section of 7.500 ± 0.002 cm diameter a distance of 3.250 ± 0.001 cm to compress the gas in the cylinder. By using the amount the gas is decreased in volume in cubic centimeters, find the uncertainty in this volume.

- Solution:

$$\begin{aligned} \delta d &= 0.002 \text{ cm} & d &= 7.500 \text{ cm} \\ \delta h &= 0.001 \text{ cm} & h &= 3.250 \text{ cm} \end{aligned}$$

$$\delta V = ?$$

The **volume** in cubic centimeters is

$$\begin{aligned} V &= \pi r^2 h \\ &= (3.14159) [7.500 \text{ cm} / 2]^2 (3.250 \text{ cm}) = 143.580 \text{ cm}^3 \end{aligned}$$

The **percent uncertainty** for diameter, height and volume are

$$\begin{aligned} u_{pd} &= (\delta d / d) \times 100 \% = (0.002 / 7.500) \times 100 \% = 0.053 \% \\ u_{ph} &= (\delta h / h) \times 100 \% = (0.001 / 3.250) \times 100 \% = 0.031 \% \\ u_{pV} &= 2(0.053 \%) + (0.031 \%) = \mathbf{0.137 \%} \quad (\text{Three decimals!}) \end{aligned}$$

The **uncertainty** in the volume of the gas in cubic centimeters is

$$\begin{aligned} \delta V &= (u_{pV} / 100 \%) V \\ &= (0.137 \% / 100 \%) (143.580 \text{ cm}^3) = 0.196705 \text{ cm}^3 \\ &= \mathbf{0.197 \text{ cm}^3} \end{aligned}$$

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References

1. College Physics
OpenStax College
Rice University, 2017.